

$A_{mn}$  is the entry in **row m** and **column n** of the matrix A.

$$1. \text{ Solve } \begin{cases} x + y + z = 6 \\ x - y + z = 2 \\ x + 2y - z = 2 \end{cases}$$

$$2. \text{ Solve } \begin{cases} x + y + z = 6 \\ x - y + z = 2 \\ x + 2y - z = 2 \end{cases}$$

$$3. \text{ Solve } \begin{cases} x + y + 0.1z = 0.1 \\ x - y + z = 5 \\ x + 2y - z = -3 \end{cases}$$

$$4. \text{ Solve } \begin{cases} x + y + z = -0.8 \\ x - y + z = 3.2 \\ x + 2y - z = -4.8 \end{cases}$$

$$5. \text{ If } \mathbf{A} = \begin{bmatrix} 1 & 0 & 3 & -2 & 4 \\ 2 & -5 & 2 & 9 & 8 \\ -7 & 8 & -6 & 5 & 2 \end{bmatrix} \text{ and } \mathbf{B} = \begin{bmatrix} 3 & -4 & 7 & 2 & -1 \\ 2 & -5 & 4 & 3 & -5 \\ 2 & -1 & -3 & -2 & 4 \end{bmatrix},$$

find the entry in row 3 column 4 of  $2\mathbf{A} - 3\mathbf{B}$ .

**For more practice:** you can also find any other single entry in  $2\mathbf{A} - 3\mathbf{B}$ .

6. Find the entry in row 3 column 2 of  $4\mathbf{A} - 5\mathbf{B}$ , if

$$\mathbf{A} = \begin{bmatrix} 1 & 2 & -3 \\ 3 & -2 & 1 \\ 3 & 4 & -5 \\ 1 & 3 & -2 \end{bmatrix} \quad \text{and} \quad \mathbf{B} = \begin{bmatrix} 3 & 1 & 2 \\ -2 & 4 & -5 \\ 2 & -3 & 7 \\ 0 & -2 & 6 \end{bmatrix}$$

**For more practice:** you can also find any other single entry in  $4\mathbf{A} - 5\mathbf{B}$ .

# Matrix Operations

$$7. \text{ If } \mathbf{A} = \begin{bmatrix} 1 & 0 & 3 & -2 & 4 \\ 2 & -5 & 2 & 9 & 8 \\ -7 & 8 & -6 & 5 & 2 \end{bmatrix} \text{ and } \mathbf{B} = \begin{bmatrix} 3 & -4 & 7 \\ -1 & 2 & 4 \\ 2 & -1 & -3 \\ -3 & -2 & 1 \\ 4 & 3 & -2 \end{bmatrix},$$

find the entry in row 2 column 3 of  $\mathbf{AB}$ .

**For more practice:** you can also find any other single entry in  $\mathbf{AB}$ .

8. Find the entry in row 3 column 2 of  $\mathbf{AB}$ , if

$$\mathbf{A} = \begin{bmatrix} 2 & -2 & 3 \\ 1 & -3 & 2 \\ 4 & -2 & 1 \\ -1 & 3 & 2 \end{bmatrix} \quad \text{and} \quad \mathbf{B} = \begin{bmatrix} 1 & -2 & -3 & 4 & -1 \\ 0 & 1 & 3 & -2 & -4 \\ 2 & -2 & 3 & -1 & -3 \end{bmatrix}$$

**For more practice:** you can also find any other single entry in  $\mathbf{AB}$ .

9. Give two  $2 \times 2$  matrices  $\mathbf{A}$  and  $\mathbf{B}$  such that  $\mathbf{AB} \neq \mathbf{BA}$ . Show that they are not equal.

10. Give the  $2 \times 3$  matrix  $\mathbf{X}$  such that for every  $2 \times 3$  matrix  $\mathbf{A}$ ,  $\mathbf{X} + \mathbf{A} = \mathbf{A} + \mathbf{X} = \mathbf{A}$ .

11. Give the  $5 \times 5$  matrix  $\mathbf{X}$  such that for every  $5 \times 5$  matrix  $\mathbf{A}$ ,  $\mathbf{XA} = \mathbf{AX} = \mathbf{A}$ .

$$12. \text{ Find the inverse of } \mathbf{A} = \begin{bmatrix} 1 & 0 & -2 \\ 0 & -1 & 0 \\ -0.2 & 0.4 & 0.5 \end{bmatrix}$$

$$13. \text{ Find the inverse of } \mathbf{A} = \begin{bmatrix} 1 & -2 & -2 \\ 1 & 0 & 0 \\ -0.2 & 1 & 0.5 \end{bmatrix}$$

**Answers:**

1.  $x = 1; y = 2; z = 3$

2.  $x = 0.1; y = 5; z = -3$

3.  $x = 2; y = -2; z = 1$

4.  $x = 0.2; y = -2; z = 1$

5.  $2 \cdot 5 - 3(-2) = 16$

**For more practice:** Other entries are given by  $2\mathbf{A} - 3\mathbf{B} = \begin{bmatrix} -7 & 12 & -15 & -10 & 11 \\ -2 & 5 & -8 & 9 & 31 \\ -20 & 19 & -3 & 16 & -8 \end{bmatrix}$

6. 31

$$4\mathbf{A} - 5\mathbf{B} = \begin{bmatrix} -11 & 3 & -22 \\ 22 & -28 & 29 \\ 2 & 31 & -55 \\ 4 & 22 & -38 \end{bmatrix}$$

7. In the instructions “row 2 column 3” means you will combine row 2 from the left factor of  $\mathbf{AB}$  with column 3 from the right factor of  $\mathbf{AB}$  as follows.

Row 2:  $2(\ ) + -5(\ ) + 2(\ ) + 9(\ ) + 8(\ )$

Fill in with column 3:  $2(7) + -5(4) + 2(-3) + 9(1) + 8(-2) = -19$

So the answer is -19

**For more practice:**  $\mathbf{AB} = \begin{bmatrix} 31 & 9 & -12 \\ 20 & -14 & -19 \\ -48 & 46 & 2 \end{bmatrix}$

8. Row 3:  $4(\ ) + (-2)(\ ) + 1(\ )$

Fill in with column 2:  $4(-2) + (-2)(1) + 1(-2) = -12$

$$\mathbf{AB} = \begin{bmatrix} 8 & -12 & -3 & 9 & -3 \\ 5 & -9 & -6 & 8 & 5 \\ 6 & -12 & -15 & 19 & 1 \\ 3 & 1 & 18 & -12 & -17 \end{bmatrix}$$

9.  $\mathbf{A} = \begin{bmatrix} 1 & 2 \\ 3 & 4 \end{bmatrix}$ ;  $\mathbf{B} = \begin{bmatrix} 5 & 6 \\ 7 & 8 \end{bmatrix}$   $\mathbf{AB} = \begin{bmatrix} 19 & - \\ - & - \end{bmatrix}$   $\mathbf{BA} = \begin{bmatrix} 23 & - \\ - & - \end{bmatrix}$

10.  $\mathbf{X} = \begin{bmatrix} 0 & 0 & 0 \\ 0 & 0 & 0 \end{bmatrix}$  This is generally denoted  $\mathbf{0}_{23}$

$$11. \mathbf{I} = \begin{bmatrix} 1 & 0 & 0 & 0 & 0 \\ 0 & 1 & 0 & 0 & 0 \\ 0 & 0 & 1 & 0 & 0 \\ 0 & 0 & 0 & 1 & 0 \\ 0 & 0 & 0 & 0 & 1 \end{bmatrix}$$

This is generally denoted  $\mathbf{I}_{55}$  or just  $\mathbf{I}_5$ , since every multiplicative identity

matrix must be square.

$$12. \mathbf{A}^{-1} = \begin{bmatrix} 5 & 8 & 20 \\ 0 & -1 & 0 \\ 2 & 4 & 10 \end{bmatrix}$$

Create  $\mathbf{A}$  in the calculator. Enter  $[\mathbf{A}]^{-1}$  using the key  $[x^{-1}]$ . The calculator will recognize that  $[\mathbf{A}]$  is a matrix instead of a number.

$$13. \mathbf{A}^{-1} = \begin{bmatrix} 0 & 1 & 0 \\ 0.5 & -0.1 & 2 \\ -1 & 0.6 & -2 \end{bmatrix}$$